

(1) Test the series: (a) $\sum_{n=1}^{\infty} (n + \frac{1}{n})$ (b) $\sum_{n=1}^{\infty} \frac{(-1)^n}{n^5 + n^2}$

(2) If $u = \cos^{-1}(\frac{x^2 + y^2}{2x + y})$. Show that: $xu_x + yu_y = -\cot u$

(3) Find the extrema of the function $f(x, y) = 2x^2 - y^2 + y(x + 1)$ subject to $2x + 3y = 2$

(4) Solve the differential equations: (a) $y' - y = e^x \cdot \sqrt{y}$ (b) $y' = -\frac{x + \sin y}{2 + x \cos y}$

(5) Show that the orthogonal trajectories of the curves $x^2 + 2y^2 = a$ are the curves $y = bx^2$

Good Luck

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